

## Dynamic Banking and the Value of Deposits

Patrick Bolton

Ye Li

Neng Wang

Jinqiang Yang

Columbia & Imperial College

OSU

Columbia

SUFE

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- A dynamic model of depository institution with endogenous risk-taking, payout policy, equity issuance, deposit-taking, and short-term borrowing
  - Deposit inflow brings uncertainty in future leverage
  - Deposit inflow destroys value for undercapitalized, risk-sensitive banks

Introduction

**Model**

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## Model: Balance Sheet

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  - If  $B_t < 0$  (holding risk-free asset),  $(A_t - B_t) / K_t = (K_t + X_t) / K_t \leq \bar{\zeta}_L$

## Model: Income Statement

$$dK_t = A_t \left[ (r + \alpha_A) dt + \sigma_A dW_t^A \right] - B_t r dt - X_t i_t dt - C(n(i_t), X_t) dt - dU_t + dF_t$$

- Deposit maintenance costs:  $C(n(i_t), X_t) dt$  (branches, customer services)
- Payout to shareholders:  $dU_t$
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$$\text{Shareholders' value: } \max_{\{A, B, i, U, F\}} \mathbb{E} \left[ \int_{t=0}^{\infty} e^{-\rho t} (dU_t - dF_t - dH_t) \right]$$

- Friction: equity issuance is subject to issuance costs  $dH_t (\geq 0)$

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## Results: Bank Equity, Issuance, and Payout Policy under Issuance Costs

- The shareholders' value  $V_t = V(K_t, X_t) = v(k_t) X_t$ 
  - Proportional cost is from the empirical literature
  - Fixed cost is calibrated to generate empirical issuance-to-book equity ratio
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  - $V_K(K_t, X_t) = v'(k_t) = 1$  only at **dividend payout boundary**  $k_t = \bar{k}$  Detail

Dynamic Optimization

Dynamic Optimization under Parametric Choices

## Results: Risk-Taking

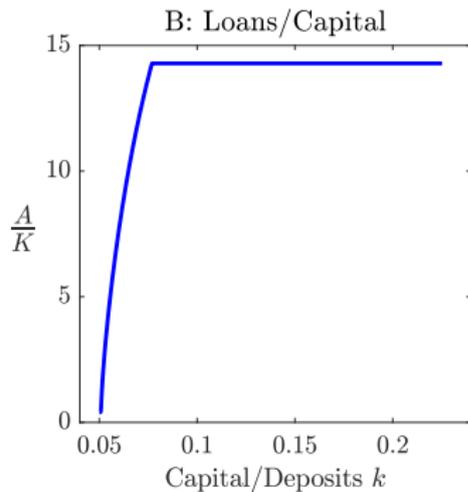
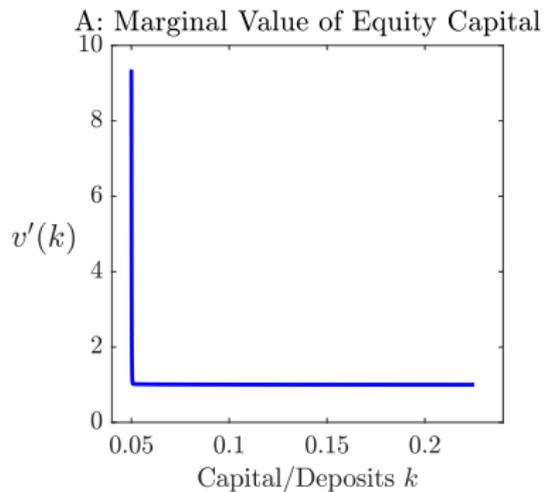
$$\frac{A}{K} = \frac{\alpha_A}{\gamma(k)\sigma_A^2} + \frac{\sigma_X}{\sigma_A}\phi$$

→ Merton portfolio choice, wealth  $K$  (equity) and risky asset  $A$  (loans)

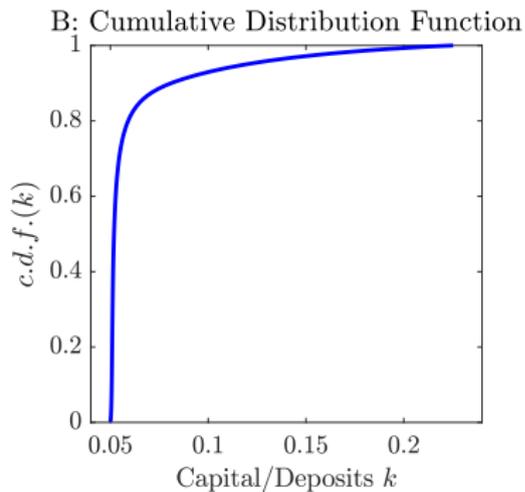
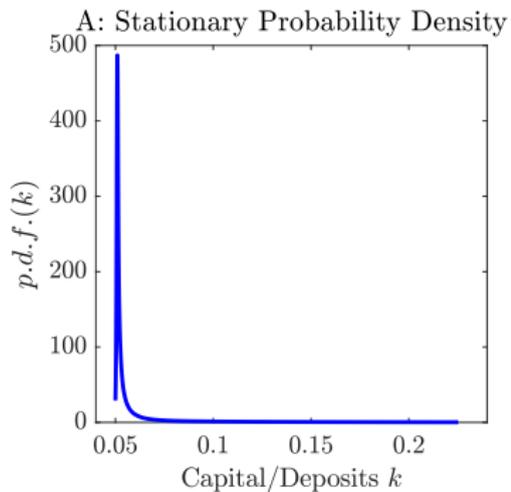
- $\gamma(k) \equiv \frac{-V_{KK}(X,K)K}{V_K(X,K)} = -\frac{v''(k)k}{v'(k)} > 0$ : concavity in  $k$  from issuance costs
- $\frac{\sigma_X}{\sigma_A}\phi$ : Hedging the “background risk” in deposit-flow uncertainty

Dynamic Optimization under Parametric Choices

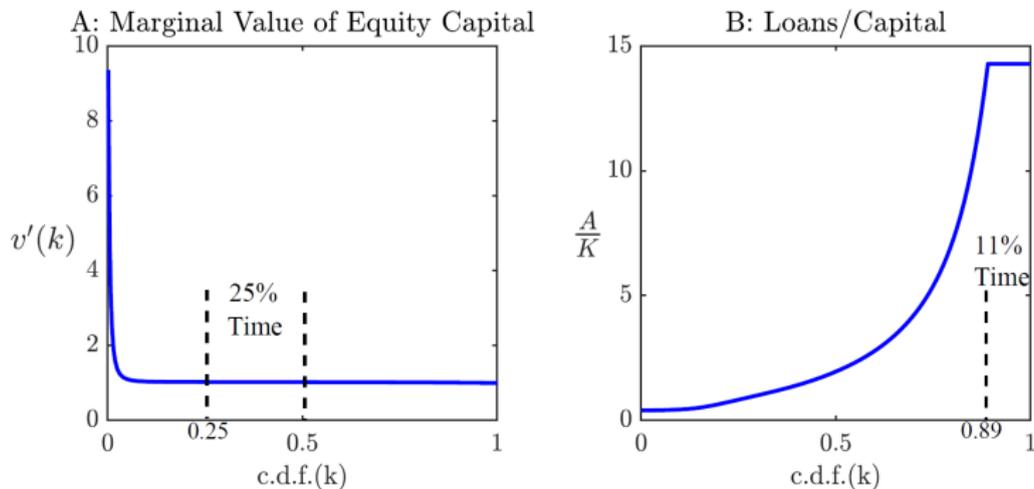
## The Value of Equity Capital and Risk-Taking



## Stationary Distribution of Capital-Deposit Ratio



## The Value of Equity Capital and Risk-Taking over the Long Run



- Capital requirement does not always bind (Begenau, Bigio, Majerovitz, Vieyra, 2019)

## Results: Optimal Deposit Rate

$$i(k) = \frac{\frac{V_X(X,K)}{V_K(X,K)} - \frac{1}{\omega}}{\theta} = \frac{\frac{v(k) - v'(k)k}{v'(k)} - \frac{1}{\omega}}{\theta}$$

→ Hayashi “investment” policy, investing in depositor/customer base

- $\frac{V_X(X,K)}{V_K(X,K)}$  is an adjusted Hayashi's Q
  - Deposit-taking (numerator) vs. return on equity (denominator)
- $\omega$ : semi-elasticity of deposit demand (Drechsler, Savov, Schnabl, 2017)
  - The rate-dependent component of deposit flow:  $n(i)dt = \omega idt$
- $\theta$ : convexity of deposit cost  $C(n(i), X) = \frac{\theta n(i)^2}{2} X$

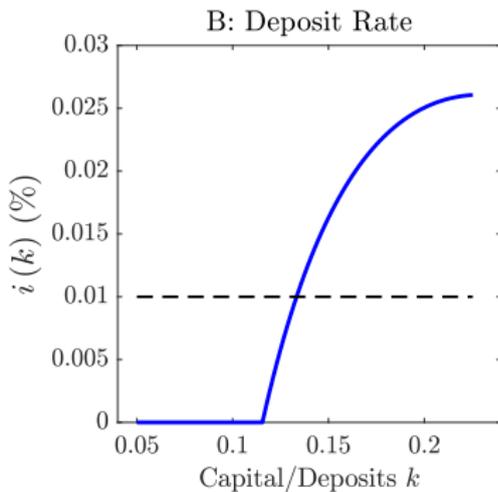
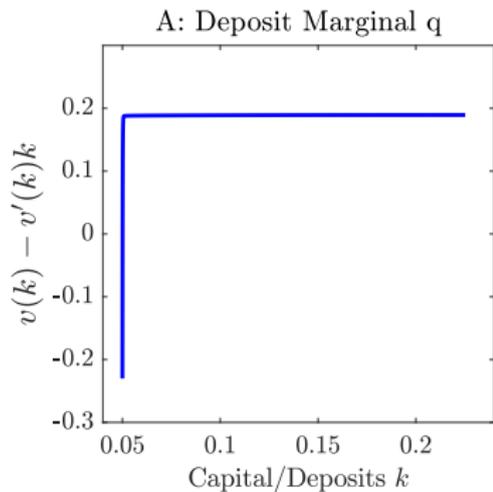
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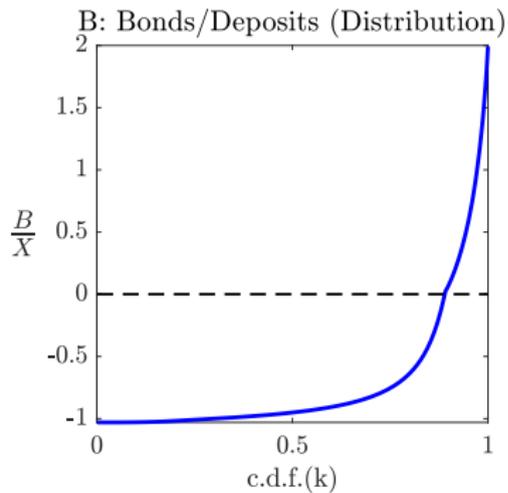
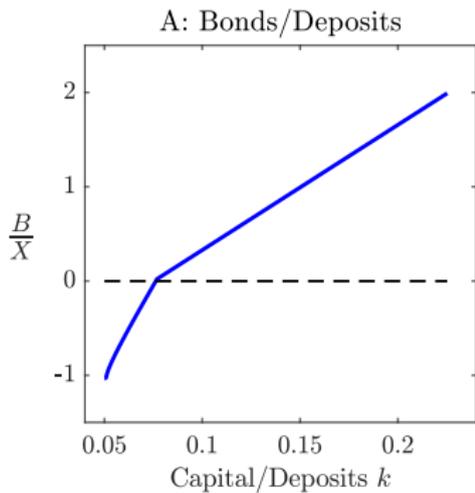
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- Deposit-rate lower bound:  $i(k) \geq 0$

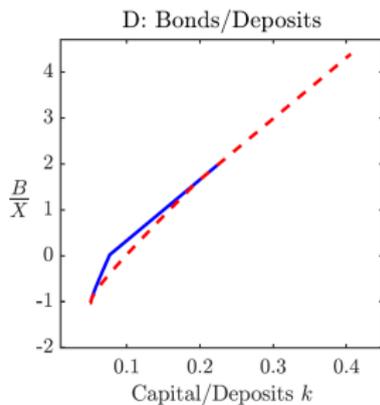
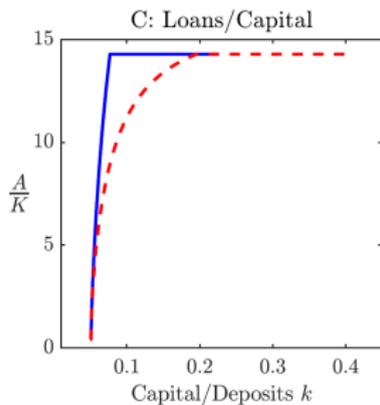
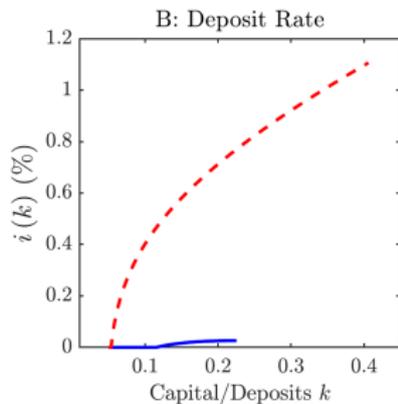
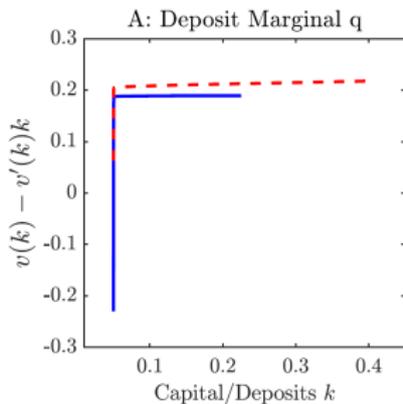
## The Value of Deposits and Optimal Deposit Rate



## Short-Term Debts



## Introducing Jump Risk in Loan Returns

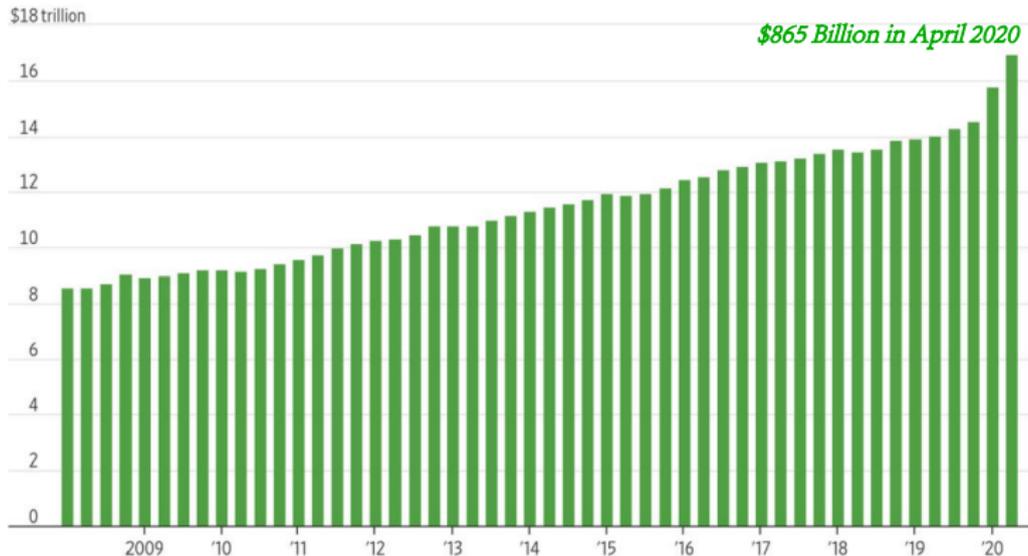


# What Happened during Covid-19 Crisis – Deposit Influx

8/30/2020

The Coronavirus Is Doing Weird Things to the Banking Industry - WSJ

## Total deposits, quarterly



Source: FDIC



## What Happened during Covid-19 Crisis – Depressed Valuation



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- A new perspective on the deposit-spread component of NIM

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  - Long-term: less frequent equity issuance  $\rightarrow$  incentive to boost ROE to compensate (occasionally incurred) issuance costs  $\downarrow \rightarrow$  risk-taking declines
  - Tightening SLR requirement  $\rightarrow$  more risk-taking in the long run (reaching for yield to compensate more frequently incurred issuance costs)
- Relaxing SLR requirement has a long-lasting positive effect on bank value
  - Less frequent equity issuance  $\rightarrow$  the bank is less risk-averse  $\rightarrow$  deposit  $q \uparrow$   
 $\rightarrow$  deposit rate  $\uparrow$  and deposit rate lower bound becomes less binding

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## Literature

- Deposits pay an interest rate below the prevailing risk-free rate
  - Banks have deposit market power (Drechsler, Savov, and Schnabl, 2017) but deposits are short-term debts
  - Deposits as means of payment: short-term debts with convenience yield

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- Marginal value of deposits is positive and banks only worry about outflows

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  - There exists uncertainty in deposit inflow/outflow (Bianchi and Bigio, 2014) but deposits are short-term debts
  - Deposits are effectively **long-term** debts as banks' deposit base is sticky (Drechsler, Savov, and Schnabl, 2018) but not random
  - Deposits are long-term contracts with **random maturity** (Diamond and Dybvig, 1983) but such risk does not appear in the no-run equilibrium
- Marginal value of deposits is positive and banks only worry about outflows
- Deposit marginal  $q$  can be negative, and inflow implies future risk

## Conclusion: Deposit Risk and Deposit Marginal $q$

- Deposit accounts commit banks to accept inflows and outflows
  - Such commitment is key to deposits serving as means of payment
  - Deposit flows are partially adjustable via the deposit rate
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- A dynamic model of depository institution with practical applications
  - (1) procyclical risk-taking; (2) procyclical short-term debt; (3) procyclical dividend payout; (4) countercyclical equity issuance

# Calibration

Table: PARAMETER VALUES

Parameters	Symbol	Value	Target
risk-free rate	$r$	1%	FRED: Fed Fund Rate
discount rate	$\rho$	4.5%	Literature
bank excess return	$\alpha_A$	0.2%	FRED: Bank ROA
asset return volatility	$\sigma_A$	10%	Literature
deposit flow (mean)	$\delta_X$	0	Literature
deposit flow (volatility)	$\sigma_X$	5%	Literature
deposit maintenance cost	$\theta$	0.5	Deposits/Total Liabilities
deposit demand semi-elasticity	$\omega$	5.3	Literature
corr. between deposit and asset shocks	$\phi$	0.8	Prob.(Capital Requirement Binds)
equity issuance fixed cost	$\psi_0$	0.1%	Issuance-to-Equity Ratio
equity issuance propositional cost	$\psi_1$	5.0%	Literature
SLR requirement parameter	$\xi_L$	20	Regulation
capital requirement parameter	$\xi_K$	14.3	Regulation

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  - 2 The increase of default probability leads to higher insurance premium
    - Equity capital is drained by the payments of deposit insurance

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- Public liquidity: Woodford, 1990; Holmström, Tirole, 1998; Krishnamurthy, Vissing-Jørgensen, 2012, 2015; Greenwood, Hanson, Stein, 2015; Drechsler, Savov, Schnabl, 2018; Moreira, Savov, 2017; Li, 2017; d'Avernas, Vandeweyer, Pariès, 2019; Liu, Schmid, Yaron, 2019; Vandeweyer, 2019

## Model: Optimization – HJB Equation

- Payout,  $dU_t$ , and issuance,  $dF_t$ , set boundaries for bank capital  $K_t$  (Details)
  - In the interior region, the value function satisfies the HJB equation

$$\begin{aligned}\rho V(X, K) = & \max_{\pi^A, i} V_X(X, K) [-X\delta_X + n(i)X] + \frac{1}{2} V_{XX}(X, K) X^2 \sigma_X^2 \\ & + V_K(X, K) (X + K) (r + \pi^A \alpha_A) - V_K(X, K) [iX + C(n(i), X)] \\ & + \frac{1}{2} V_{KK}(X, K) (X + K)^2 (\pi^A \sigma_A)^2 + V_{XK}(X, K) (X + K) \pi^A \sigma_A X \sigma_X \phi.\end{aligned}$$

- The bank controls  $\pi^A = A / (X + K)$  and  $i$ 
  - Given states  $X$  and  $K$ , B/S identity,  $A = X + B + K$ , implies  $B$

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[Optimal Payout and Issuance](#)

[Optimal  \$\pi^A\$](#)

[Optimal  \$i\$](#)

## Model: Equity Issuance and Payout

- The bank raises equity only if

$$V(X, K + dF_t) - V(X, K) \geq dF_t + dH_t = \psi_0 X + (1 + \psi_1) M_t.$$

- Capital raised:  $dF_t = M_t$ , given by  $V_K(X, K + M_t) = 1 + \psi_1$

- Issuance costs:  $dH_t = \psi_0 X + \psi_1 M_t$

- Fix cost scaled by  $X$  for value function be homogeneous in  $X$

- The bank pays out dividend only if

$$V(X, K) - V(X, K - dU_t) \leq dU_t \text{ i.e., } V_K(X, K) \leq 1.$$

- Optimality and smooth-pasting condition:  $V_{KK}(X, K) = 0$

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## Model: Optimal Risk-Taking

$$\frac{A}{K} = \min \left\{ \frac{\alpha_A + \epsilon(X, K) \sigma_A \sigma_X \phi}{\gamma(X, K) \sigma_A^2}, \bar{\xi}_K \right\}$$

*Endogenous Risk Aversion:*  $\gamma(X, K) \equiv \frac{-V_{KK}(X, K) K}{V_K(X, K)}$

*Hedging Motive:*  $\epsilon(X, K) \equiv \frac{V_{XK}(X, K) X}{V_K(X, K)}$

$\gamma$ : Concavity,  $V_{KK}(X, K) < 0$ , from the equity issuance costs

$\epsilon$ : Hedging motive from background risk in the randomness of deposit flow

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## Model: Optimal Deposit Rate

$$V_X(X, K) n'(i) = V_K(X, K) [1 + C_n(n(i), X) n'(i)] .$$

*LHS* : Marginal benefit of adding deposits

*RHS* : Marginal cost of paying deposit rates and deposit maintenance costs  
(from adding more deposits)

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## Model: Solution under Homogeneity

- State space transformation:  $(K_t, X_t) \rightarrow (k_t, X_t)$  where

$$k_t = \frac{K_t}{X_t}$$

- Value function:  $V(X, K) = v(k)X$  and HJB equation (ODE)

$$\begin{aligned} \rho v(k) = \max_{\pi^A, i} & [v(k) - v'(k)k] (-\delta_X + \omega i) + \frac{1}{2} v''(k) k^2 \sigma_X^2 \\ & + v'(k) (1+k) (r + \pi^A \alpha_A) + \frac{1}{2} v''(k) (1+k)^2 (\pi^A \sigma_A)^2 \\ & - v'(k) \left[ i + \frac{\theta}{2} (\omega i)^2 \right] - v''(k) k (1+k) \pi^A \sigma_A \sigma_X \phi. \end{aligned}$$

- The bank controls  $\pi^A = A/(X+K)$  and  $i$ 
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